# Book For Maharashtra Public Service Commission



# **MPSC Police Constable Mathematics Sample Paper**



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| 1 | (1)   | What parcentage of numbers from | 1 to 70 have 1 or 9 in the unit's digit? |
|---|-------|---------------------------------|--|
| М | L I I | What percentage of numbers from | 1 to /v have I of / in the unit suight.  |

[A] 1

[B] 14

[C] 20

[D] 21

## Answer: [C]

#### **Explanation:**

Clearly, the numbers which have 1 or 9 in the unit's digit, have squares that end in the digit 1. Such numbers from 1 to 70 are 1, 9, 11, 19, 21, 29, 31, 39, 41, 49, 51, 59, 61, 69.

Number of such number =14

 $\therefore \text{ Required percentage} = \left(\frac{14}{70} \times 100\right)_{\%} = 20\%.$ 

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# (2) If A = x% of y and B = y% of x, then which of the following is true?

[A] A is smaller than B.

[B] A is greater than B

[C] Relationship between A and B cannot be determined.

[D] If x is smaller than y, then A is greater than B.

[E] None of these

#### Answer: [E]

#### **Explanation:**

$$x\% \text{ of } y = \left(\frac{x}{100} \times y\right) = \left(\frac{y}{100} \times x\right) = y\% \text{ of } x$$

 $\cdot \cdot \cdot A = B.$ 

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# (3) A batsman scored 110 runs which included 3 boundaries and 8 sixes. What percent of his total score did he make by running between the wickets?

[A] 45%

[B] 45<sup>5</sup>/<sub>11</sub>%

[C]
54<sup>6</sup>/<sub>11</sub>%

[D] 55%

## Answer: [B]

# **Explanation:**

Number of runs made by running =  $110 - (3 \times 4 + 8 \times 6)$ 

= 110 - (60)

 $\therefore \text{ Required percentage} = \left(\frac{50}{110} \times 100\right)_{\% = 4511} \frac{5}{110} \%$ 

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## (4) A fruit seller had some apples. He sells 40% apples and still has 420 apples. Originally, he had:

[A] 588 apples

[B] 600 apples

[C] 672 apples

#### Answer: [D]

## **Explanation:**

Suppose originally he had x apples.

Then, 
$$(100 - 40)\%$$
 of  $x = 420$ .

$$\Rightarrow \frac{60}{100} \times x = 420$$

$$\Rightarrow x = \left(\frac{420 \times 100}{60}\right) = 700.$$

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#### (5) If 20% of a = b, then b% of 20 is the same as:

- [A] 4% of a
- [B] 5% of a
- [C] 20% of a
- [D] None of these

#### Answer: [A]

#### **Explanation:**

20% of 
$$a = b \implies \frac{20}{100}a = b$$
.

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# (6) If a - b = 3 and $a^2 + b^2 = 29$ , find the value of ab.

- [A] 10
- [B] 12
- [C] 15
- [D] 18

#### Answer: [A]

#### **Explanation:**

$$2ab = (a^{2} + b^{2}) - (a - b)^{2}$$

$$= 29 - 9 = 20$$

$$\Rightarrow ab = 10.$$

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# (7) To fill a tank, 25 buckets of water is required. How many buckets of water will be required to fill the same tank if the capacity of the bucket is reduced to two-fifth of its present?

- [A] 10
- [B] 35
- [C] 62.5
- [D] Cannot be determined
- [E] None of these

## Answer: [C]

#### **Explanation:**

Let the capacity of 1 bucket = x. Then, the capacity of tank = 25x.

New capacity of bucket = 
$$\frac{2}{5}x$$

$$\therefore \text{ Required number of buckets} = \frac{25x}{(2x/5)}$$

$$= \left( \frac{5}{25x} \times \frac{5}{2x} \right)$$

$$=\frac{125}{2}$$

$$=62.5$$

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## (8) A fires 5 shots to B's 3 but A kills only once in 3 shots while B kills once in 2 shots. When B has missed 27 times, A has killed:

- [A] 30 birds
- [B] 60 birds
- [C] 72 birds
- [D] 90 birds

## Answer: [A]

#### **Explanation:**

Let the total number of shots be x. Then,

Shots fired by A = 
$$\frac{5}{8}x$$

Shots fired by B = 
$$\frac{3}{8}x$$

Killing shots by A = 
$$\frac{1}{3}$$
 of  $\frac{5}{8}x = \frac{5}{24}x$ 

Shots missed by B = 
$$\frac{1}{2}$$
 of  $\frac{3}{8}x = \frac{3}{16}x$ 

$$\frac{3x}{16} = 27 \text{ or } x = \left(\frac{27 \times 16}{3}\right) = 144.$$

Birds killed by A = 
$$\frac{5x}{24}$$
 =  $\left(\frac{5}{24} \times 144\right)$  = 30.

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#### (9) A person crosses a 600 m long street in 5 minutes. What is his speed in km per hour?

- [A] 3.6
- [B] 7.2
- [C] 8.4
- [D] 10

#### Answer: [B]

## **Explanation:**

Speed = 
$$\left(\frac{600}{5 \times 60}\right)_{\text{m/sec.}}$$

= 2 m/sec.

Converting m/sec to km/hr (see important formulas section)

$$=\left(2 \times \frac{18}{5}\right) \text{km/hr}$$

= 7.2 km/hr.

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# (10) A man complete a journey in 10 hours. He travels first half of the journey at the rate of 21 km/hr and second half at the rate of 24 km/hr. Find the total journey in km.

| [R] | 224 | 1/m |
|-----|-----|-----|

[C] 230 km

[D] 234 km

Answer: [B]

Explanation: 
$$\frac{(1/2)x}{21} + \frac{(1/2)x}{24} = 10$$

$$\Rightarrow \frac{x}{21} + \frac{x}{24} = 20$$

$$\Rightarrow 15x = 168 \times 20$$
$$\Rightarrow x = \left(\frac{168 \times 20}{15}\right) = 224 \text{ km}.$$

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# (11) A man on tour travels first 160 km at 64 km/hr and the next 160 km at 80 km/hr. The average speed for the first 320 km of the tour is:

- [A] 35.55 km/hr
- [B] 36 km/hr
- [C] 71.11 km/hr
- [D] 71 km/hr

Answer: [C]

**Explanation:** 

Total time taken = 
$$\left(\frac{160}{64} + \frac{160}{80}\right)_{hrs.} = \frac{9}{2}$$
 hrs.

$$\therefore$$
 Average speed =  $\left(320 \times \frac{2}{9}\right)_{\text{km/hr}}$  = 71.11 km/hr.

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# (12) A car travelling with $\frac{5}{7}$ of its actual speed covers 42 km in 1 hr 40 min 48 sec. Find the actual speed of the car.

[A]  $17\frac{6}{7}$  km/hr

- [B] 25 km/hr
- [C] 30 km/hr
- [D] 35 km/hr

Answer: [D]

**Explanation:** 

Time taken = 1 hr 40 min 48 sec = 1 hr  $40\frac{4}{5}$  min =  $1\frac{51}{75}$  hrs =  $\frac{126}{75}$  hrs.

Let the actual speed be x km/hr.  
Then, 
$$\frac{5}{7}x \times \frac{126}{75} = 42$$

$$\Rightarrow x = \left(\frac{42 \times 7 \times 75}{5 \times 126}\right) = 35 \text{ km/hr.}$$

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#### (13) In covering a distance of 30 km, Abhay takes 2 hours more than Sameer. If Abhay doubles his speed, then he would take 1 hour less than Sameer. Abhay's speed is:

|     | - |      |
|-----|---|------|
| IR1 | 6 | kmph |

[C] 6.25 kmph

[D] 7.5 kmph

Answer: [A]

#### **Explanation:**

Let Abhay's speed be x km/hr.

Then, 
$$\frac{30}{x} - \frac{30}{2x} = 3$$

$$\Rightarrow 6x = 30$$

$$\Rightarrow x = 5 \text{ km/hr}.$$

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(14) Tea worth Rs. 126 per kg and Rs. 135 per kg are mixed with a third variety in the ratio 1:1:2. If the mixture is worth Rs. 153 per kg, the price of the third variety per kg will be:

[A] Rs. 169.50

[B] Rs. 170

[C] Rs. 175.50

[D] Rs. 180

Answer: [C]

#### **Explanation:**

Since first and second varieties are mixed in equal proportions.

So, their average price = Rs. 
$$\left(\frac{126 + 135}{2}\right)$$
 = Rs. 130.50

So, the mixture is formed by mixing two varieties, one at Rs. 130.50 per kg and the other at say, Rs. x per kg in the ratio 2:2, i.e., 1:1. We have to find

By the rule of alligation, we have:

Cost of 1 kg of 1st kind

Cost of 1 kg of 1 st kind Cost of 1 kg tea of 
$$2^{nd}$$
 kind Rs. 130.50 Rs.  $x$ 

$$\therefore \frac{x-153}{22.50}=1$$

$$\Rightarrow x - 153 = 22.50$$
$$\Rightarrow x = 175.50$$

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(15) A vessel is filled with liquid, 3 parts of which are water and 5 parts syrup. How much of the mixture must be drawn off and replaced with water so that the mixture may be half water and half syrup?

Answer: [C]

#### **Explanation:**

Suppose the vessel initially contains 8 litres of liquid. Let x litres of this liquid be replaced with water.

Quantity of water in new mixture =  $\left(3 - \frac{1}{8} + x\right)$  litres

Quantity of syrup in new mixture =  $\left(5 - \frac{5x}{8}\right)$  litres

$$\therefore \left(3 - \frac{3x}{8} + x\right) = \left(5 - \frac{5x}{8}\right)$$

$$\Rightarrow$$
 5x + 24 = 40 - 5x

$$\Rightarrow 10x = 16$$

$$\Rightarrow x = \frac{8}{5}$$

So, part of the mixture replaced =  $\left(\frac{8}{5} \times \frac{1}{8}\right) = \frac{1}{5}$ .

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(16) In what ratio must a grocer mix two varieties of pulses costing Rs. 15 and Rs. 20 per kg respectively so as to get a mixture worth Rs. 16.50 kg?

- [A] 3:7
- [B] 5:7
- [C] 7:3
- [D] 7:5

Answer: [C]

**Explanation:** 

By the rule of alligation:

Cost of 1 kg pulses of  $1^{st}$  kind

Cost of 1 kg pulses of 2<sup>nd</sup> kind

Rs. 15

Mean Price Rs. 16.50

3.50

1.50

 $\therefore$  Required rate = 3.50 : 1.50 = 7 : 3.

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(17) The cost of Type 1 rice is Rs. 15 per kg and Type 2 rice is Rs. 20 per kg. If both Type 1 and Type 2 are mixed in the ratio of 2:3, then the price per kg of the mixed variety of rice is:

[A] Rs. 18

[B] Rs. 18.50

[C] Rs. 19

[D] Rs. 19.50

Answer: [A]

#### **Explanation:**

Rs. 15

Let the price of the mixed variety be Rs. x per kg.

By rule of alligation, we have:

Cost of 1 kg of Type 1 rice

Cost of 1 kg of Type 2 rice

Mean Price

Rs. 20

Rs. x

$$(20 - x)$$
  $(x - 15)$ 

$$\therefore \frac{(20-x)}{(x-15)} = \frac{2}{3}$$

$$\Rightarrow$$
 60 - 3 $x$  = 2 $x$  - 30

$$\Rightarrow 5x = 90$$

$$\Rightarrow x = 18.$$

| Find the ratio in which rice | at Rs. 7.20 a kg he mived wi | h rice at Rs. 5.70 a kg to produce | a mixture worth Rs 630 a kg |
|------------------------------|------------------------------|------------------------------------|-----------------------------|

[A] 1:3

[B] 2:3

[C] 3:4

[D] 4:5

Answer: [B]

#### **Explanation:**

By the rule of alligation:

Cost of 1 kg of 1<sup>st</sup> kind 720 p

Cost of 1 kg of 2<sup>nd</sup> kind 570 p

90

Mean Price 630 p

60

 $\therefore$  Required ratio = 60: 90 = 2:3.

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# (19) A car owner buys petrol at Rs.7.50, Rs. 8 and Rs. 8.50 per litre for three successive years. What approximately is the average cost per litre of petrol if he spends Rs. 4000 each year?

[A] Rs. 7.98

[B] Rs. 8

[C] Rs. 8.50

[D] Rs. 9

Answer: [A]

#### **Explanation:**

Total quantity of petrol consumed in 3 years 
$$= \left(\frac{4000}{7.50} + \frac{4000}{8} + \frac{4000}{8.50}\right) \text{ litres}$$
$$= 4000 \left(\frac{2}{15} + \frac{1}{8} + \frac{2}{17}\right) \text{ litres}$$
$$= \left(\frac{76700}{51}\right) \text{ litres}$$

Total amount spent = Rs. (3 x 4000) = Rs. 12000.

• Average cost = Rs. 
$$\left(\frac{12000 \times 51}{76700}\right)$$
 = Rs.  $\frac{6120}{767}$  = Rs. 7.98

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# (20) A library has an average of 510 visitors on Sundays and 240 on other days. The average number of visitors per day in a month of 30 days beginning with a Sunday is:

[A] 250

[B] 276

[C] 280

[D] 285

#### Answer: [D]

# **Explanation:**

Since the month begins with a Sunday, to there will be five Sundays in the month.

Required average 
$$= \left(\frac{510 \times 5 + 240 \times 25}{30}\right)$$
$$= \frac{8550}{30}$$

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